



# Efficient and Precise Points-to Analysis: Modeling the Heap by Merging Equivalent Automata

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**UNSW**  
SYDNEY



# A New Points-to Analysis Technique for Object-Oriented Programs

# Points-to Analysis

- Determines
  - “which objects a variable can point to?”

# Uses of Points-to Analysis

## Clients

- Security analysis
- Bug detection
- Compiler optimization
- Program verification
- Program understanding
- ...

## Tools



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## Tools



Call Graph

# Existing Call Graph Construction

- On-the-fly construction  
(run with points-to analysis)
  - Precise
  - Inefficient

# Existing Call Graph Construction

- On-the-fly construction  
(run with points-to analysis)
  - Precise
  - Inefficient
- 3-object-sensitive points-to analysis
  - Very precise
  - Adopted by, e.g.,   

# 3-Object-Sensitive Points-to Analysis

- Analyze Java programs
  - Intel Xeon E5 3.70GHz, 128GB of memory
  - Time budget: 5 hours (18000 secs)

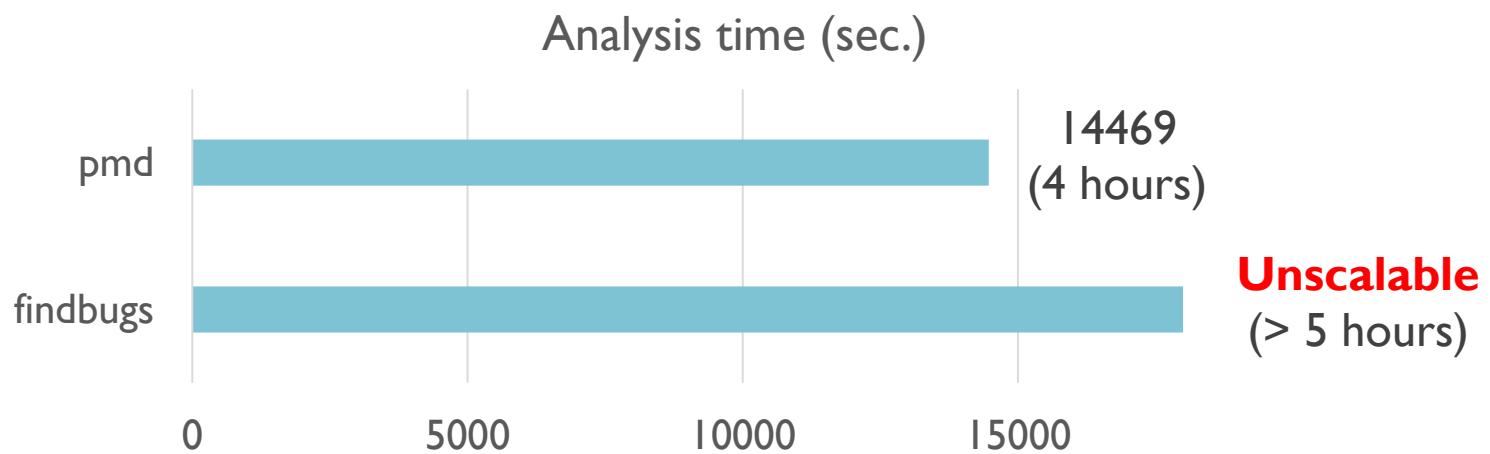


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# Two Mainstreams of Points-to Analysis Techniques

- Model control-flow
- Model data-flow

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  - Context-sensitivity
    - Call-site-sensitivity (PLDI'04, PLDI'06)
    - Object-sensitivity (ISSTA'02, TOSEM'05, SAS'16)
    - Type-sensitivity (POPL'11)
    - ...
- Model data-flow

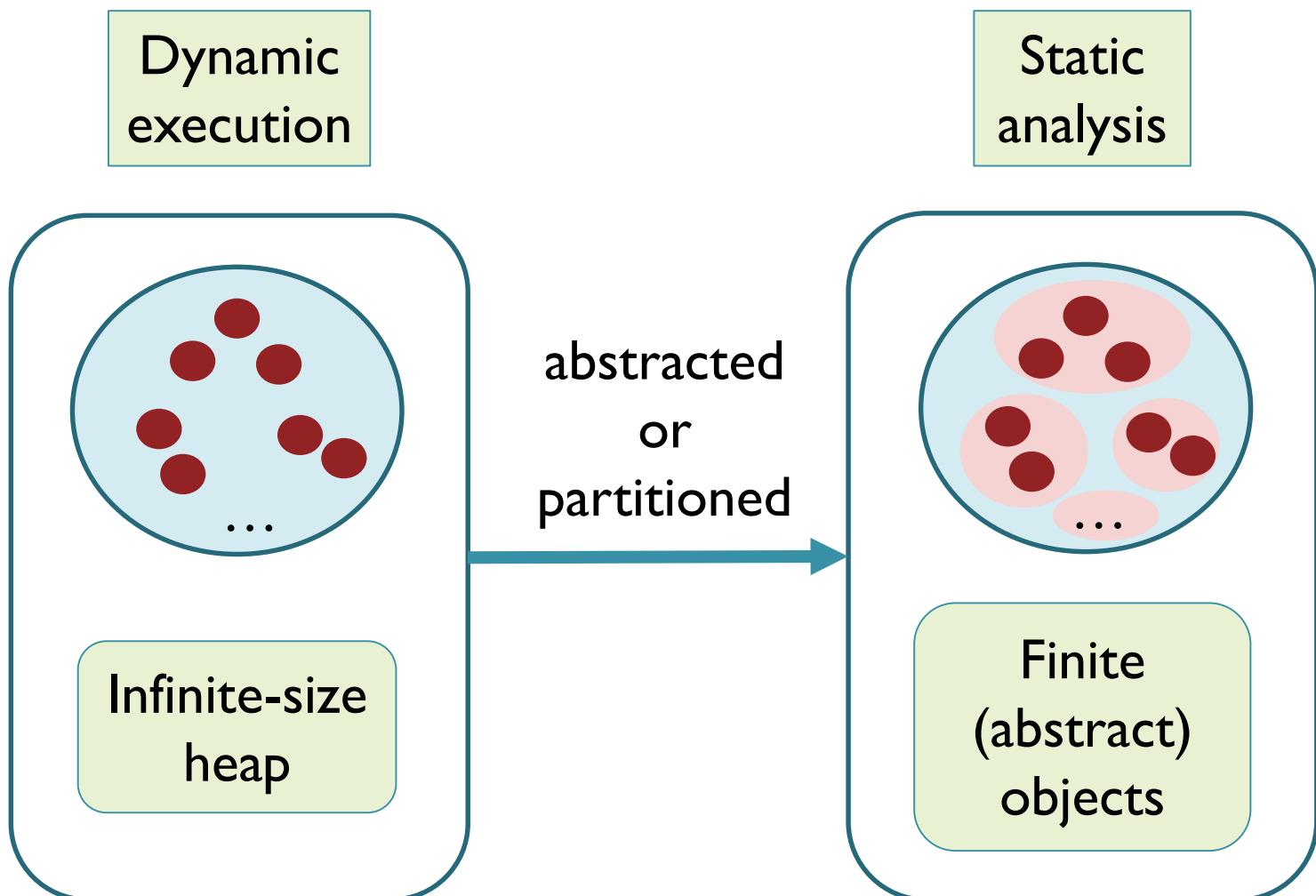
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  - Heap abstraction
    - Allocation-site abstraction
    - Type-based abstraction
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  - **Heap abstraction**
    - Allocation-site abstraction
    - Type-based abstraction
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# Heap Abstraction



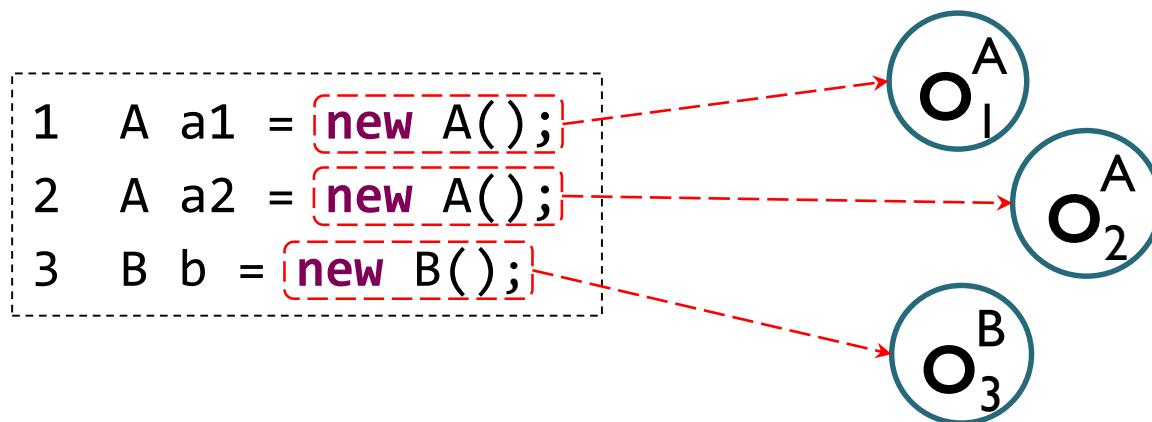
# Allocation-Site Abstraction

- One object per **allocation site**

```
1 A a1 = new A();  
2 A a2 = new A();  
3 B b = new B();
```

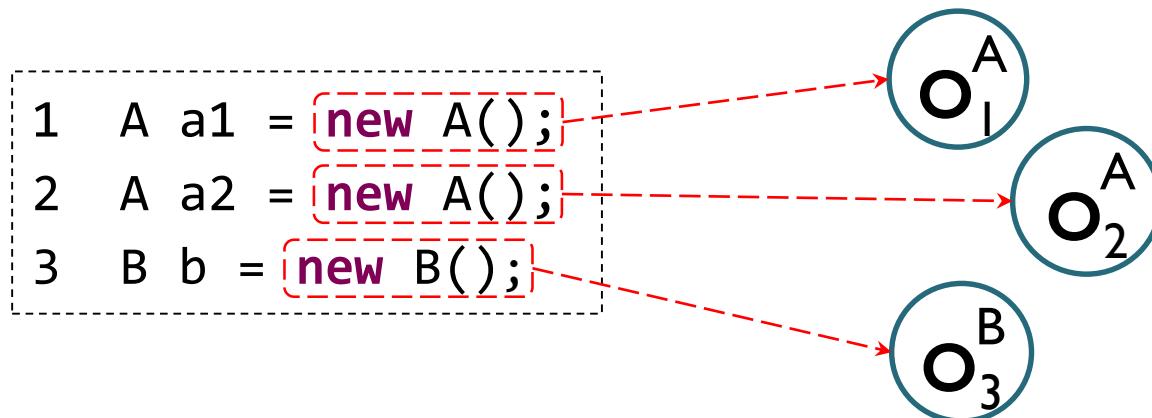
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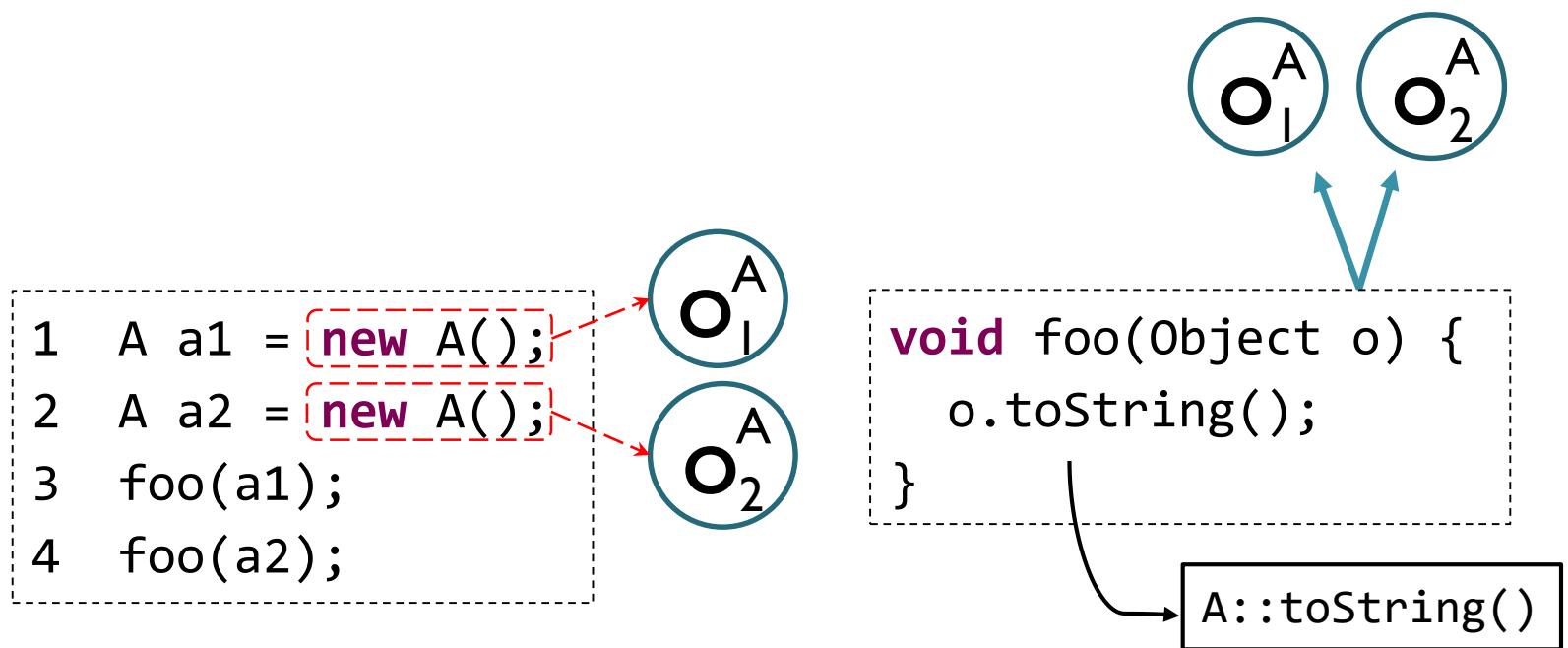
# Allocation-Site Abstraction

- One object per **allocation site**
  - Adopted by **all** mainstream points-to analyses



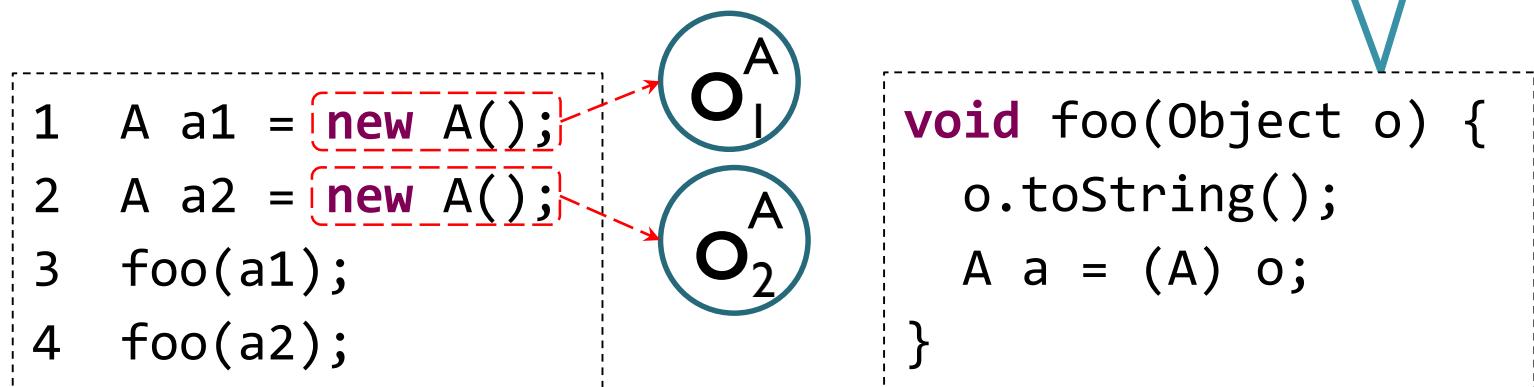
# Allocation-Site Abstraction

- **Over-partition** for call graph construction



# Allocation-Site Abstraction

- **Over-partition** for **type-dependent clients**
  - Call graph construction
  - Devirtualization
  - May-fail casting
  - ...



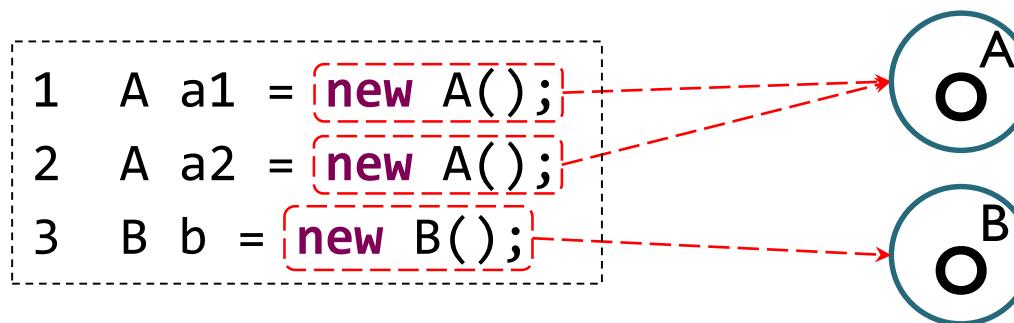
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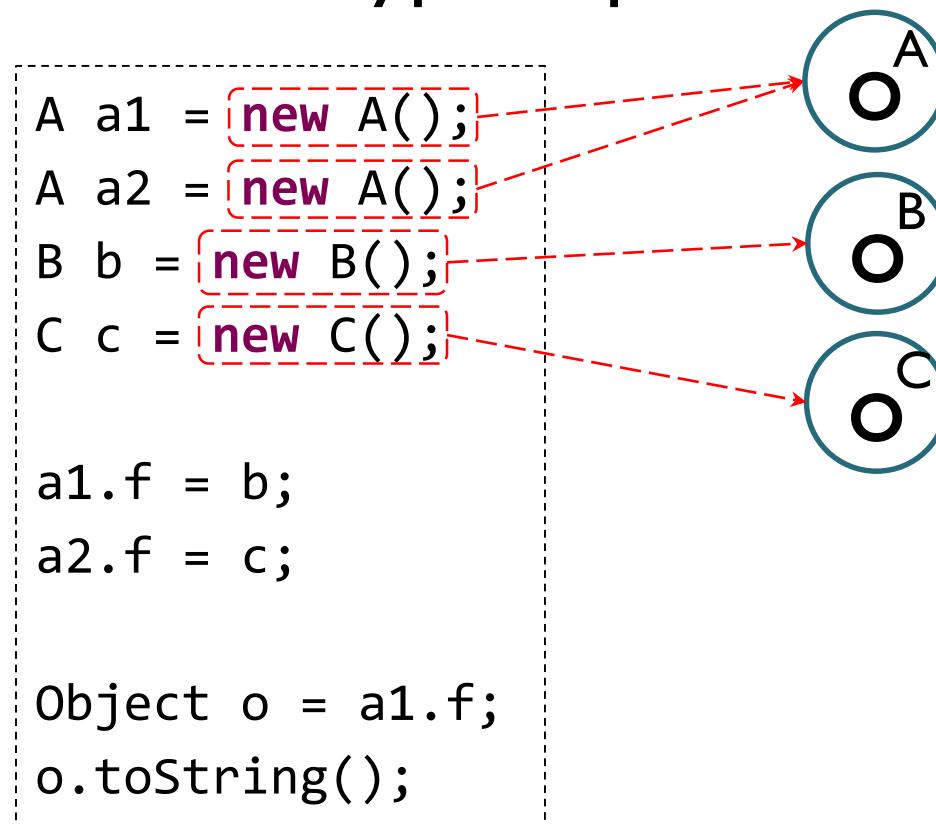
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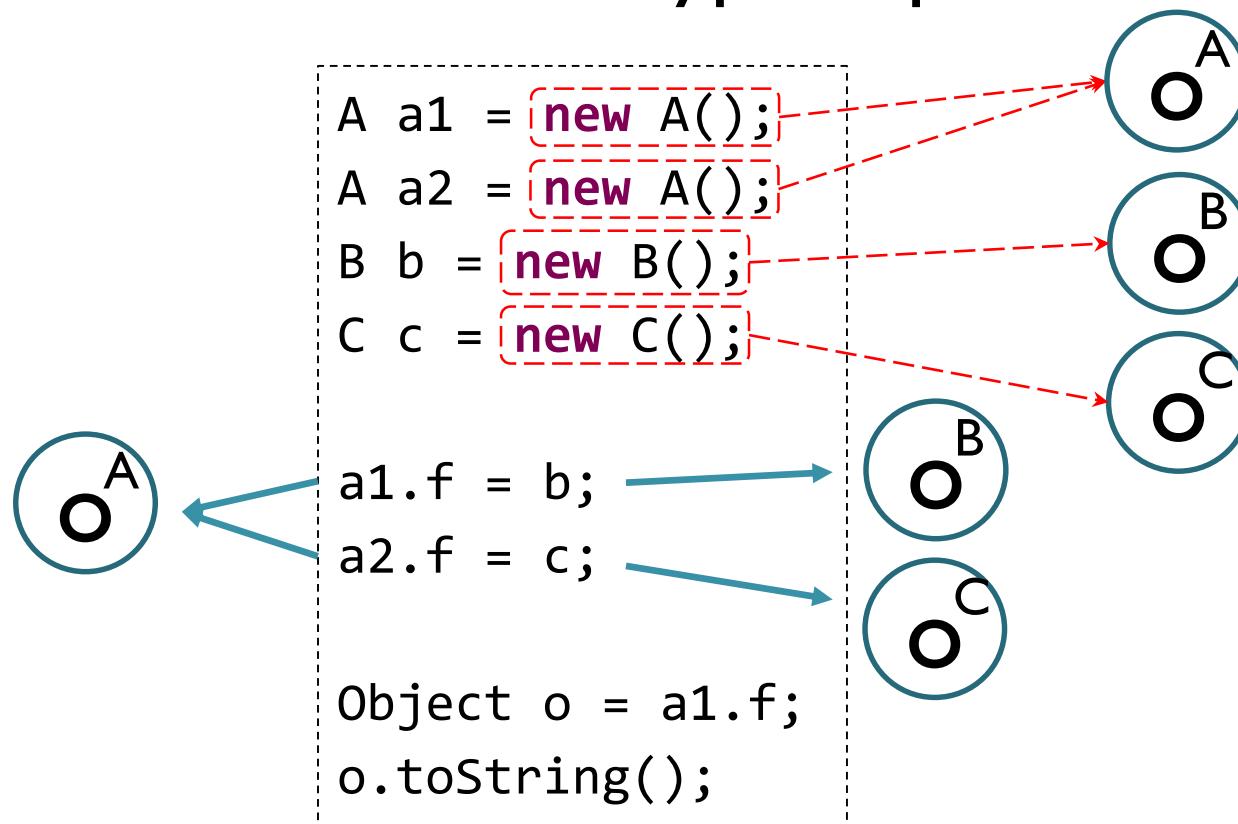
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- Precision loss for type-dependent clients



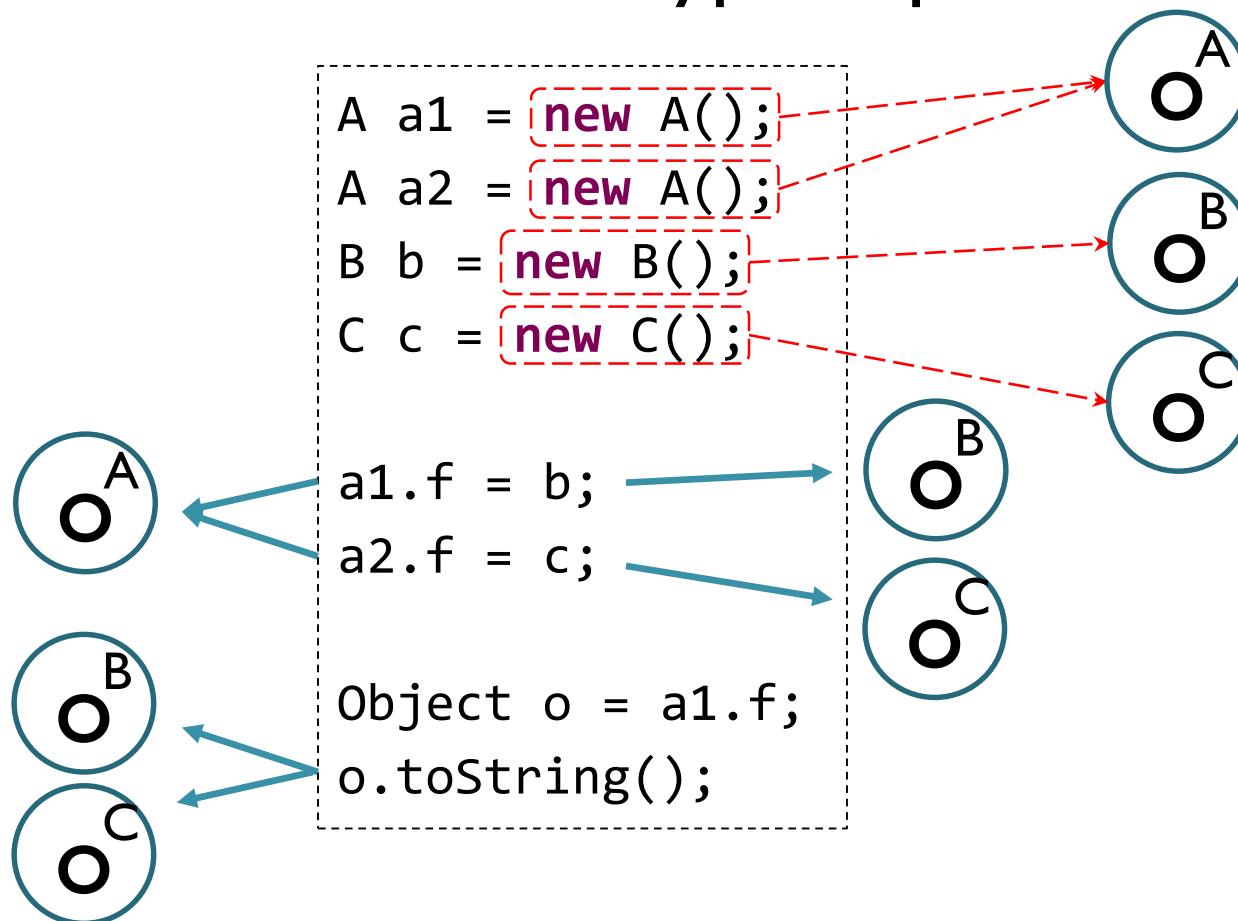
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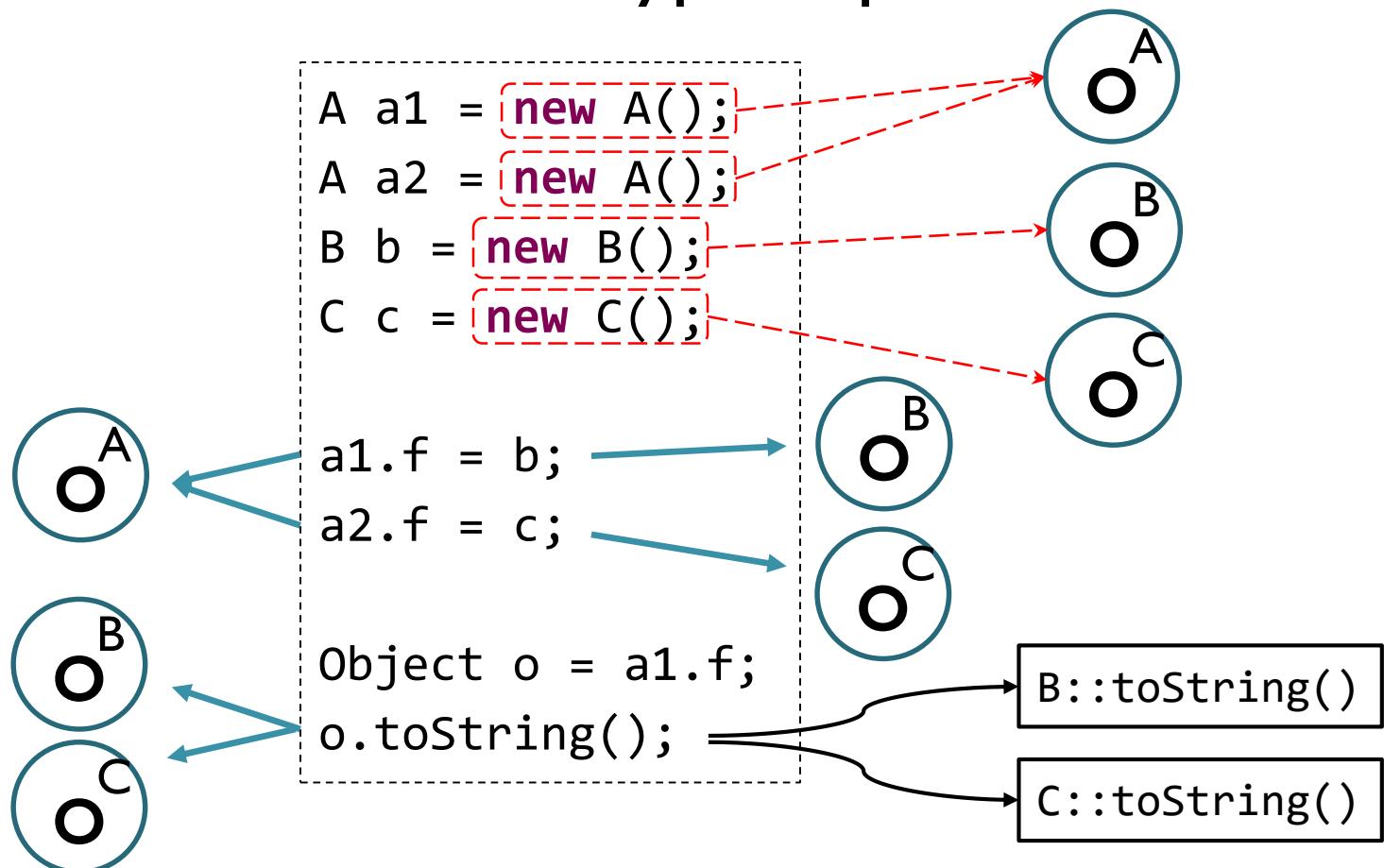
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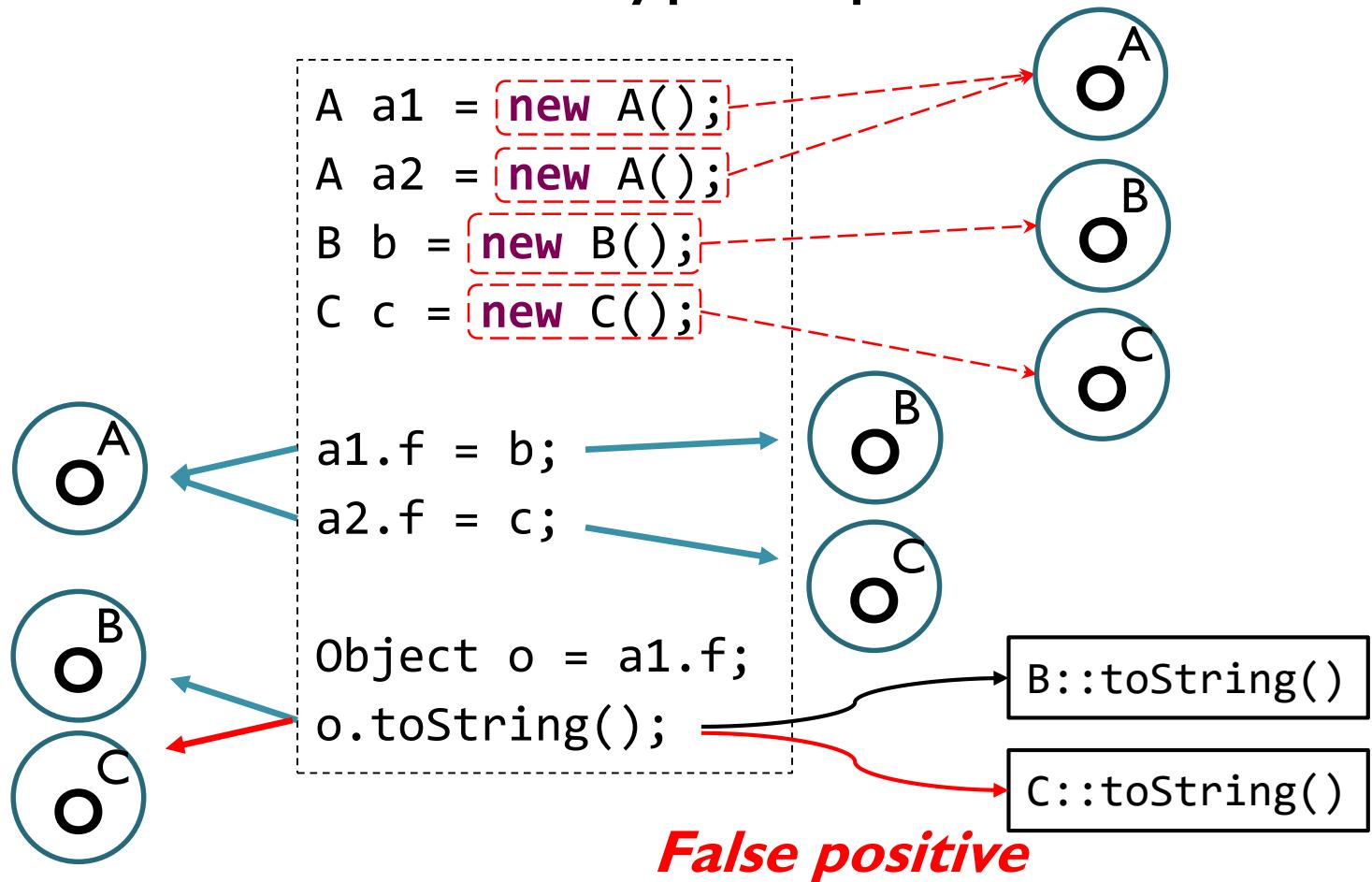
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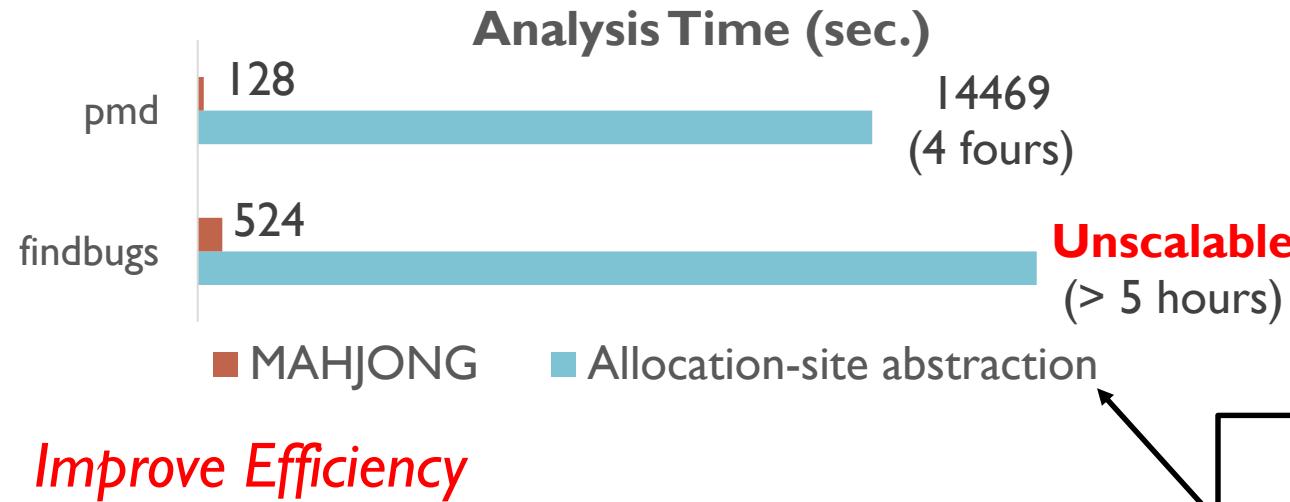
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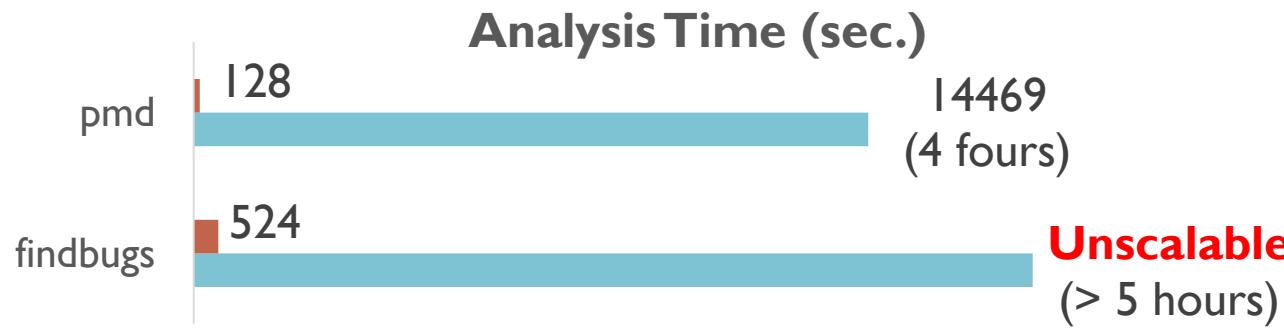
**Our Goal:**  
**Improve Efficiency**  
**Preserve Precision**

# MAHJONG: A New Heap Abstraction

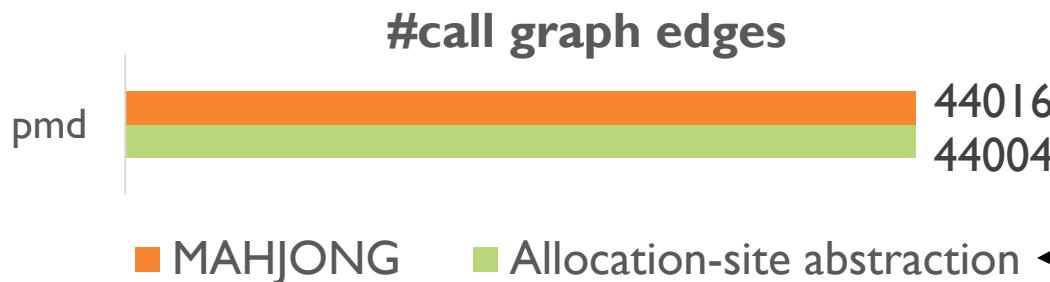


Adopted by  
**all** mainstream  
points-to analyses

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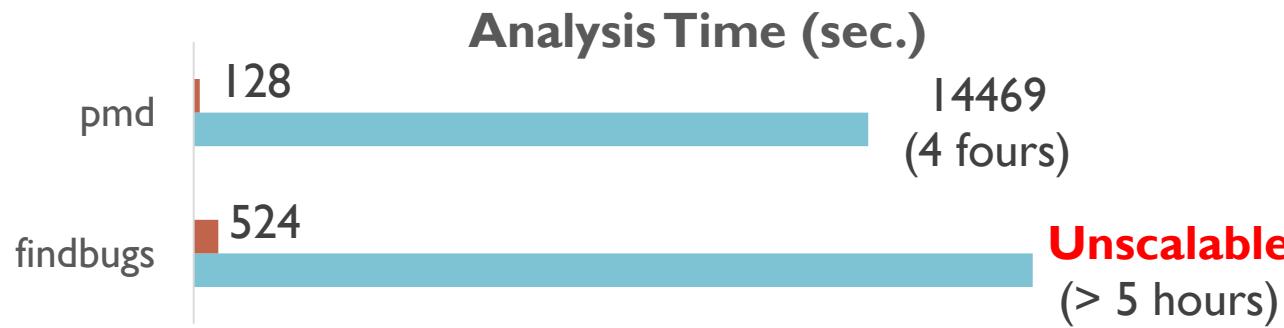
*Improve Efficiency*



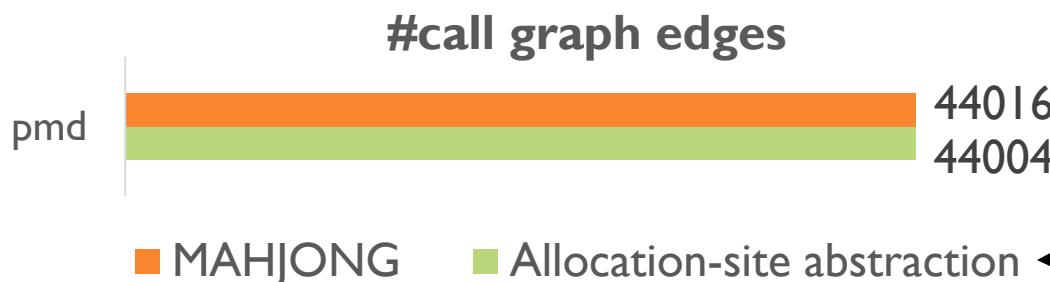
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# MAHJONG: A New Heap Abstraction



*Improve Efficiency*



*Preserve Precision*

How?

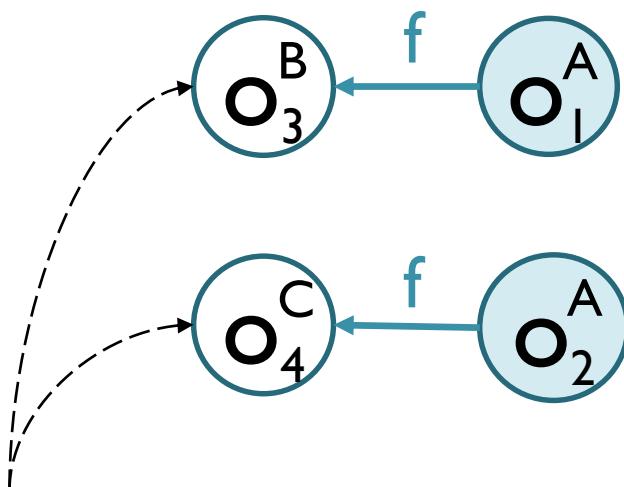
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Merging Objects  **alleviate** Over-Partition

Blindly Merging Objects  **cause** Precision Loss

Merging Objects alleviate → Over-Partition

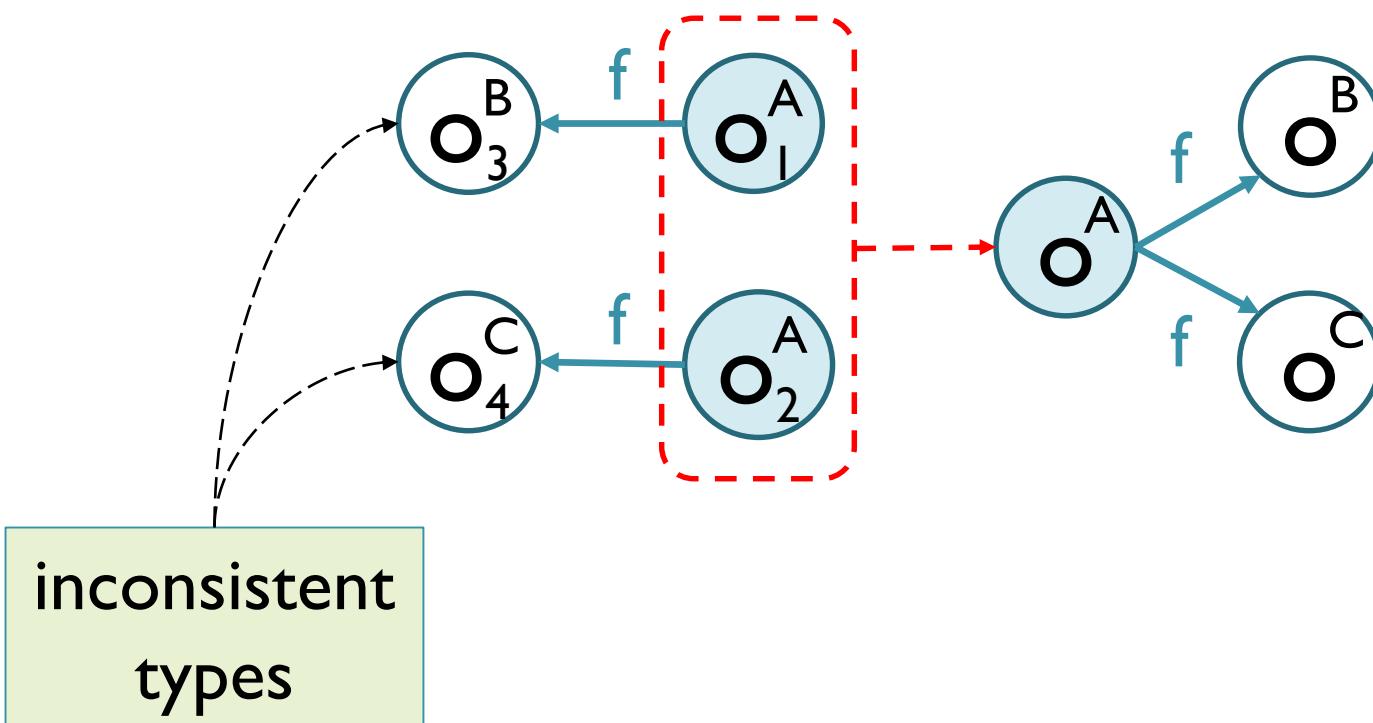
Blindly Merging Objects cause → Precision Loss



inconsistent  
types

Merging Objects alleviate → Over-Partition

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# Type-Consistent Objects

- **Definition**

$O_i^T$  and  $O_j^T$  are **type-consistent objects**,

if for every sequence of field names,

$$\overline{f} = f_1 \cdot f_2 \cdot \dots \cdot f_n :$$

$O_i^T \cdot \overline{f}$  and  $O_j^T \cdot \overline{f}$  point to the objects of the  
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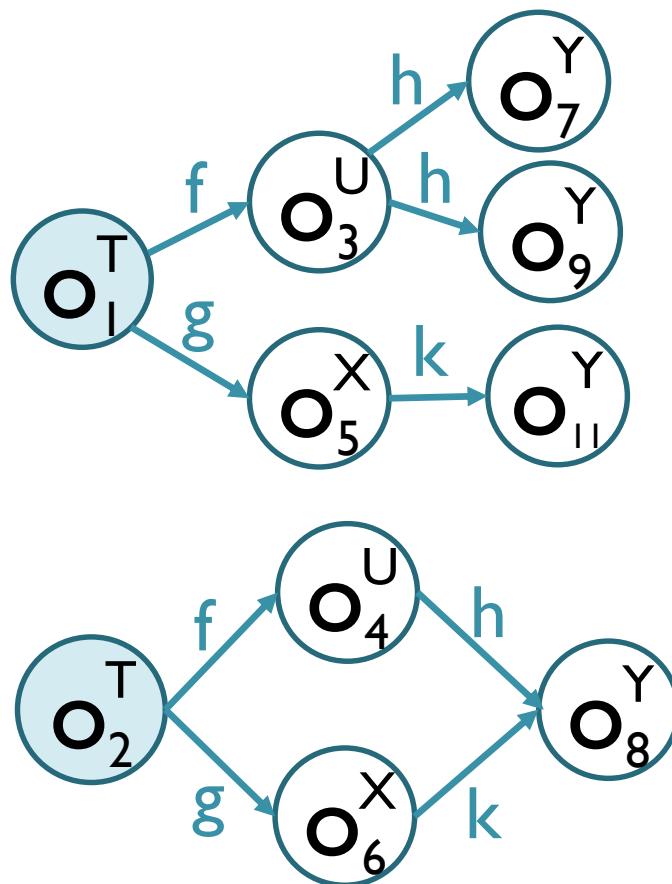
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MAHJONG only merges **type-consistent objects**

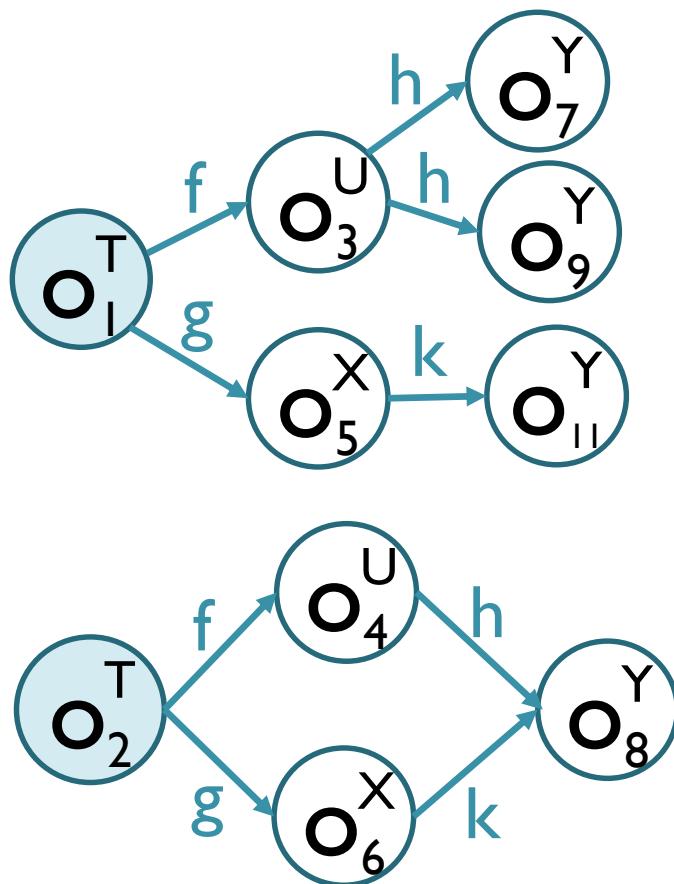
# Type-Consistent Objects

- Example



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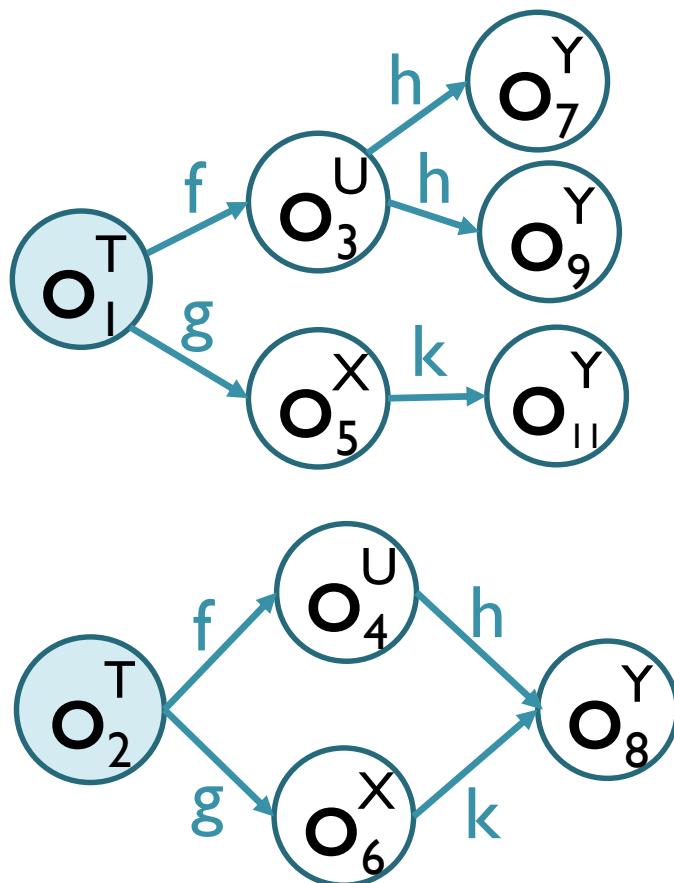
- Example



	$O_1^T$	$O_2^T$
.f	U	U
.f.h	Y	Y
.g	X	X
.g.k	Y	Y

# Type-Consistent Objects

- Example



⋮

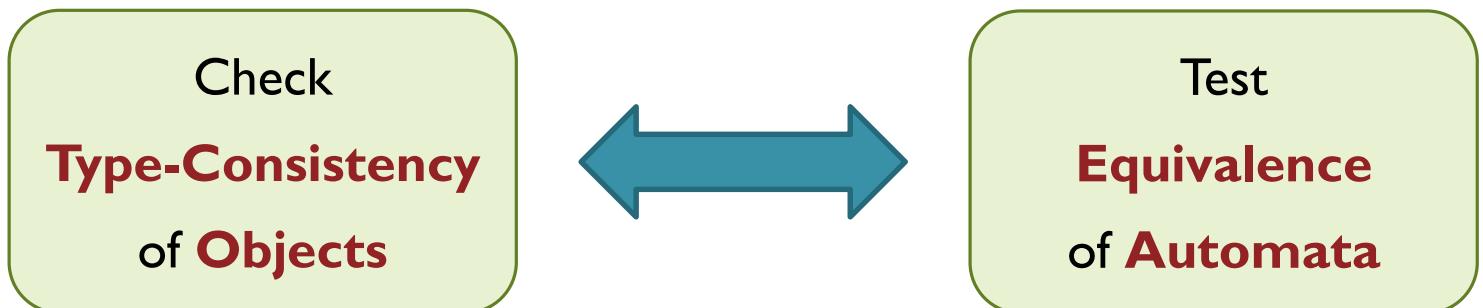
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⋮

$O_1^T$  and  $O_2^T$  are  
type-consistent objects

# How to Check Type-Consistency?

# Our Solution: Sequential Automata



# Sequential Automata

- 6-tuple  $(Q, \Sigma, \delta, q_0, \Gamma, \gamma)$ , where:
  - $Q$  is a set of states
  - $\Sigma$  is a set of input symbols
  - $\delta$  is the next-state map:  $Q \times \Sigma \rightarrow \mathcal{P}(Q)$
  - $q_0$  is the initial state
  - $\Gamma$  is a set of output symbols
  - $\gamma$  is the output map:  $Q \rightarrow \Gamma$

Check  
**Type-Consistency**  
of **Objects**



Test  
**Equivalence**  
of **Automata**

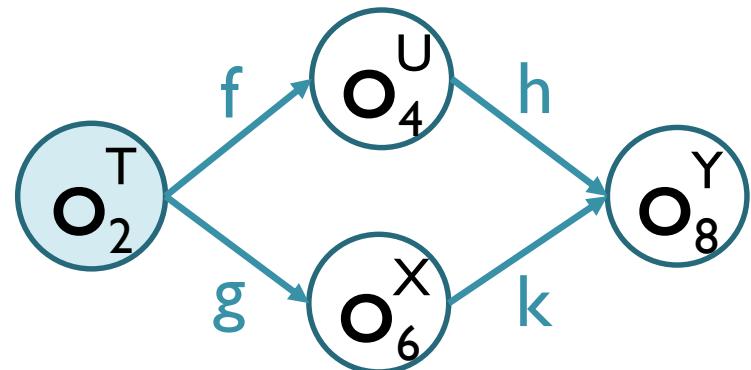
# How?

## Objects

- A set of **objects**
- A set of **field names**
- The **field points-to map**
- The **object** to be checked
- A set of **types**
- The **object-to-type** map

## Automata

- $Q$ : a set of **states**
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## Objects

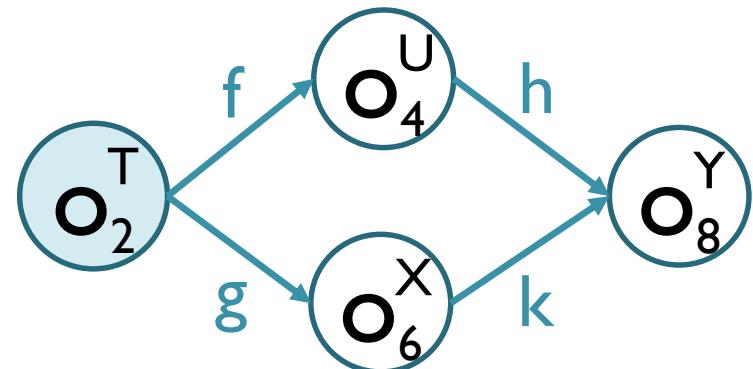
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objects  $\leftrightarrow$  states

$O_2^T, O_4^U, O_6^X, O_8^Y$



## Objects

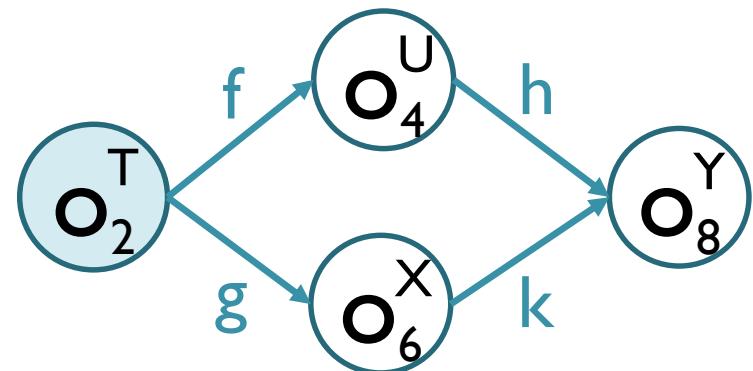
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field names  $\leftrightarrow$  input symbols

f, g, h, k



## Objects

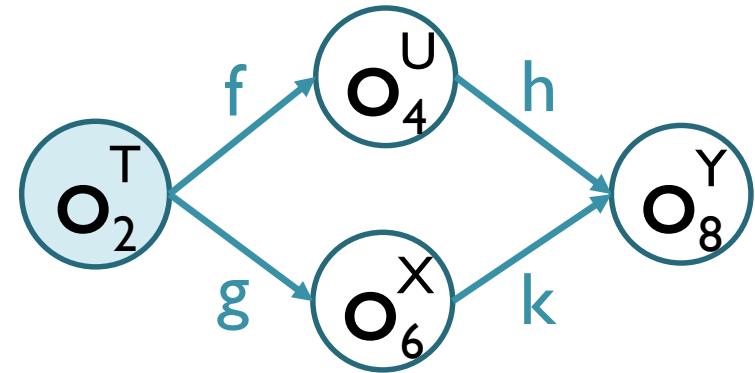
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field points-to map  $\leftrightarrow$  next-state map

$O_2^T$	f	$O_4^U$
$O_2^T$	g	$O_6^X$
$O_4^U$	h	$O_8^Y$
$O_6^X$	k	$O_8^Y$



## Objects

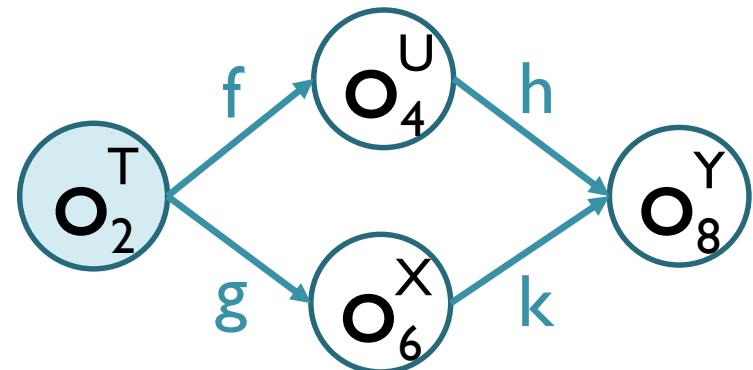
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checked object  $\leftrightarrow$  initial state

$O_2^T$



## Objects

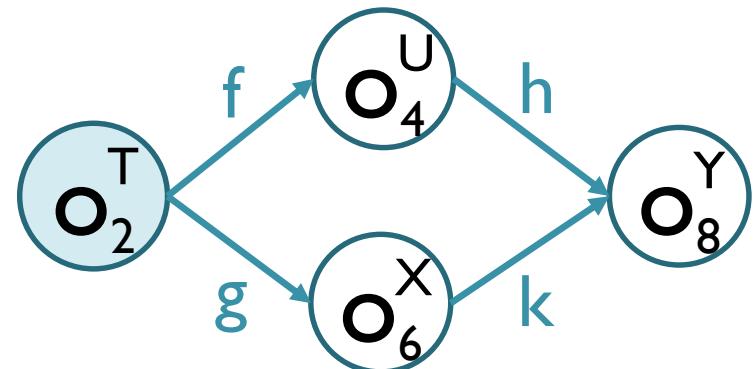
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types  $\leftrightarrow$  output symbols

T, U, X, Y



## Objects

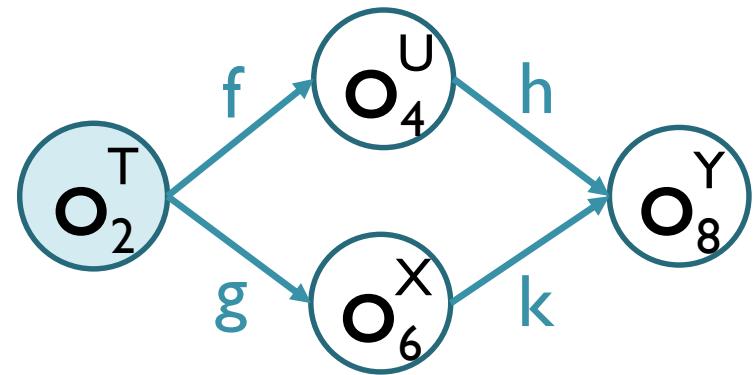
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object-to-type map  $\leftrightarrow$  output map

$O_2^T$	T
$O_4^U$	U
$O_6^X$	X
$O_8^Y$	Y



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Test  
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# Test Equivalence of Automata

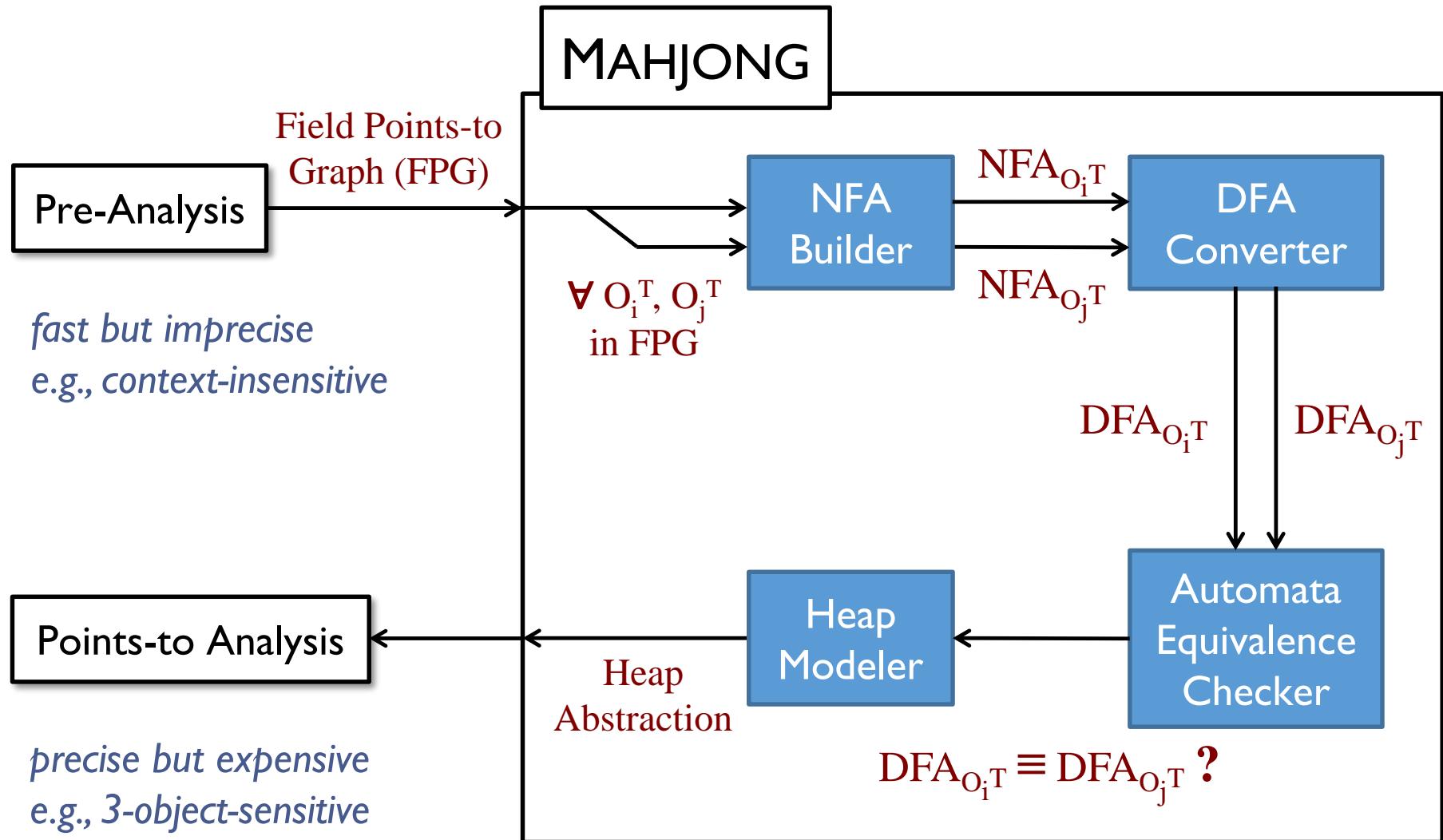
- Hopcroft-Karp algorithm\*
  - Almost linear in terms of  $|Q_{\text{larger}}|$
  - $Q_{\text{larger}}$ : set of states of the larger automaton

\* J. E. Hopcroft and R. M. Karp, *A linear algorithm for testing equivalence of finite automata*, Technical Report 71-114, 1971



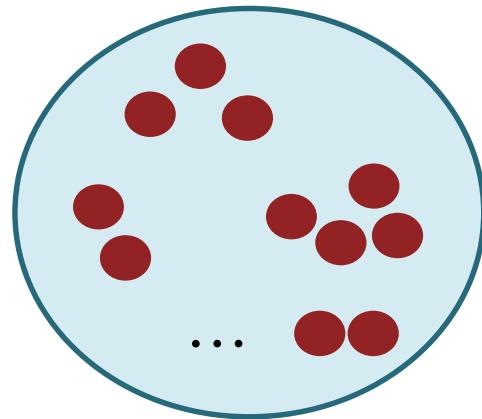
# Methodology (MAHJONG)

# Overview



## Original

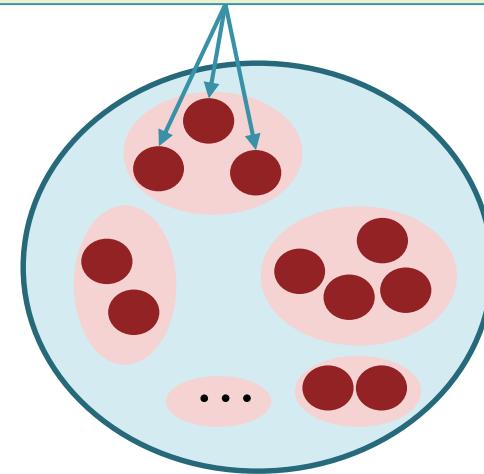
- Allocation-site heap abstraction



## New

- MAHJONG heap abstraction

type-consistent objects



# Working with Points-to Analysis

# Implementation



- 1500 LOC of Java in total
- Integrated with Doop
- Can also be easily integrated to other points-to analysis frameworks

# Evaluation

# Evaluation - Research Questions

- RQ1: MAHJONG's effectiveness as a pre-analysis
- RQ2: MAHJONG-based points-to analysis

# RQ I: MAHJONG's Effectiveness as A Pre-Analysis

- Efficiency
  - Is MAHJONG lightweight for large programs?
- Heap partitioning
  - Can MAHJONG avoid heap over-partition?

# Pre-Analysis: Efficiency

	antlr	fop	luindex	pmd	chart	checkstyle	xalan	bloat	lusearch	JPC	findbugs	eclipse
<b>CI</b>	44.1	34.7	26.2	44.8	37.7	89.6	66.6	38.7	41.4	58.9	90.6	174.1
<b>FPG</b>	1.3	0.7	0.8	1.4	2.4	2.3	3.0	1.2	0.8	2.1	4.6	15.5
<b>MAHJONG</b>	1.3	1.1	1.1	1.5	1.9	4.0	3.1	1.7	1.0	4.5	3.2	211.4
<b>Total</b>	46.7	36.5	28.1	47.7	42.0	95.9	72.7	41.6	43.2	65.5	98.4	211.0

**CI:** Context-Insensitive points-to analysis

**FPG:** Read Field Points-to Graph

**MAHJONG:** Check automata equivalence, build heap abstraction

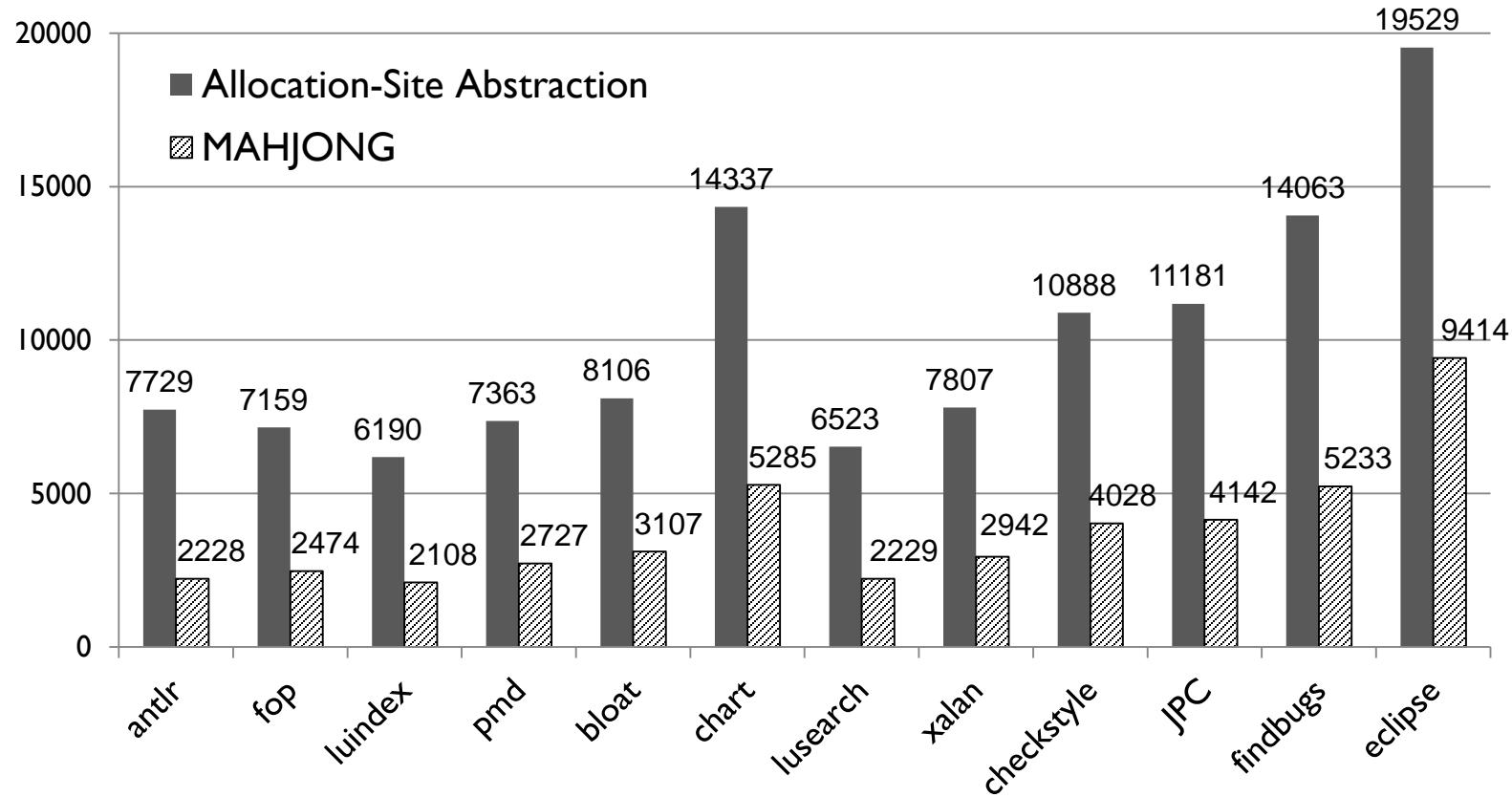
In total: 1 minute

MAHJONG itself: 3.8 seconds

Each program (on average)

# Pre-Analysis: Heap Partition

Number of abstract objects created by the  
allocation-site abstraction and MAHJONG



Average reduction: 62%

# RQ2: MAHJONG-Based Points-to Analysis

- Efficiency
  - Can MAHJONG accelerate points-to analysis?
- Precision
  - Can MAHJONG preserve precision for type-dependent clients?

# Evaluated Points-to Analyses

- 5 mainstream context-sensitive points-to analyses:
  1. 2-call-site-sensitive analysis
  2. 2-type-sensitive analysis
  3. 3-type-sensitive analysis
  4. 2-object-sensitive analysis
  5. 3-object-sensitive analysis
- Time budget: 5 hours

DoOP

# Evaluated Clients

- Call graph construction
- Devirtualization
- May-fail casting

# MAHJONG-Base Points-to Analysis: Results

- Efficiency
  - Most precise  
(3-object-sensitive)  
***Speedup: 131X***
- Precision
  - Call graph: **-0.02%**
  - Devirtualization: **-0.29%**
  - May-fail casting: **-0%**

# MAHJONG-Base Points-to Analysis: Results

- Efficiency

Most precise  
(3-object-sensitive)  
***Speedup: 131X***

On average  
***Speedup: 15X***

- Precision

Call graph: -0.02%  
Devirtualization: -0.29%  
May-fail casting: -0%

Call graph: -0.02%  
Devirtualization: -0.18%  
May-fail casting: -0.03%

# MAHJONG-Base Points-to Analysis: Results

- Efficiency

Most precise  
(3-object-sensitive)  
**Speedup: 131X**

On average  
**Speedup: 15X**

- Precision

Call graph: -0.02%  
Devirtualization: -0.29%  
May-fail casting: -0%

Call graph: -0.02%  
Devirtualization: -0.18%  
May-fail casting: -0.03%

For checkstyle, xalan, lusearch, JPC, findbugs

3-object-sensitive analysis:

- **without MAHJONG**, unscalable (**> 5 hours**)
- **with MAHJONG**, finish in **1 min ~ 84 mins** (**33 minutes on average**)

# Conclusion

- MAHJONG
  - Improve significantly the efficiency of different point-to analyses
    - Call-site-, object- and type-sensitivity
  - Preserve almost the same precision for type-dependent clients
- Direct impact
  - Benefit many program analyses where call graphs are required



# Thank you!